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Ferrimagnetism in EuFe₄As₁₂ revealed by Eu-153 NMR and As-75 NQR measurements

Abstract

Filled skutterudite compound EuFe₄As₁₂ shows the highest magnetic ordering temperature of TC=154K among Eu-based skutterudite compounds, but its magnetic ground state has not been determined yet. Here, we performed ¹⁵³Eu nuclear magnetic resonance (NMR) and ⁷⁵As nuclear quadrupole resonance (NQR) measurements on EuFe₄As₁₂ to reveal its magnetic ground state as well as the physical properties from a microscopic point of view. From the temperature and magnetic field dependence of ¹⁵³Eu NMR spectrum in the magnetically ordered state, we found that the Eu ions are in Eu²⁺ state with a nearly 7 μ B corresponding to S=7/2 spins. Combined with the magnetization measurements, which show the reduced saturation moments of 4.5 μ B/f.u., we determined the ground magnetic structure in EuFe₄As₁₂ to be ferrimagnetic where the Eu²⁺ 4f and the Fe3d ordered moments are ferromagnetically aligned in each sublattice but the moments between the sublattices are antiferromagnetically aligned. We also found the local distortion at the Eu site from the cubic symmetry in the magnetically ordered state. The relationship between the rattling motion of Eu atoms and the local symmetry of the Eu ions is discussed. From the ⁷⁵As NQR nuclear spin-lattice relaxation time measurements as well as ¹⁵³Eu NMR measurements, we found that the 4f electrons of the Eu ions are well described by the local moment picture in both the magnetic and paramagnetic metallic states.

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Ferrimagnetism in $\text{EuFe}_4\text{As}_{12}$ revealed by ^{153}Eu NMR and ^{75}As NQR measurements

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Filled skutterudite compound $\text{EuFe}_4\text{As}_{12}$ shows the highest magnetic ordering temperature of $T_C = 154$ K among Eu-based skutterudite compounds, but its magnetic ground state has not been determined yet. Here, we performed ^{153}Eu nuclear magnetic resonance (NMR) and ^{75}As nuclear quadrupole resonance (NQR) measurements on $\text{EuFe}_4\text{As}_{12}$ to reveal its magnetic ground state as well as the physical properties from a microscopic point of view. From the temperature and magnetic field dependence of ^{153}Eu NMR spectrum in the magnetically ordered state, we found that the Eu ions are in Eu^{2+} state with a nearly $7 \mu_B$ corresponding to $S = 7/2$ spins. Combined with the magnetization measurements, which show the reduced saturation moments of $4.5 \mu_B/\text{f.u.}$, we determined the ground magnetic structure in $\text{EuFe}_4\text{As}_{12}$ to be ferrimagnetic where the $\text{Eu}^{2+} 4f$ and the $\text{Fe } 3d$ ordered moments are ferromagnetically aligned in each sublattice but the moments between the sublattices are antiferromagnetically aligned. We also found the local distortion at the Eu site from the cubic symmetry in the magnetically ordered state. The relationship between the rattling motion of Eu atoms and the local symmetry of the Eu ions is discussed. From the ^{75}As NQR nuclear spin-lattice relaxation time measurements as well as ^{153}Eu NMR measurements, we found that the $4f$ electrons of the Eu ions are well described by the local moment picture in both the magnetic and paramagnetic metallic states.

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I. INTRODUCTION

The interplay of $4f$ and itinerant electrons in rare-earth containing metallic systems provides fascinating physical phenomena such as superconductivity, ferromagnetism, antiferromagnetism, non-Fermi-liquid behavior, heavy-fermion states, and so on [1–6]. Among many materials bearing rare-earth elements, the europium-containing Fe-based superconducting material EuFe_2As_2 stands as one of the interesting materials since, with carrier doping or pressure application, the system shows the coexistence of superconductivity and magnetism originating from Eu $4f$ moments, where the magnetism of itinerant Fe moments also plays an important role [7–10]. EuFe_2As_2 at ambient pressure exhibits two distinct magnetic phase transitions at $T = 189$ K and 19 K. The first magnetic order is a spin density wave [stripe-type antiferromagnetic (AFM) state] associated with the itinerant Fe moments while the second one is due to $\text{Eu}^{2+} 4f$ moments, making an A-type AFM structure where the Eu ordered moments are ferromagnetically aligned in the ab plane but the moments in adjacent layers along the c axis are antiferromagnetically aligned [7]. Although the Eu and Fe moments order at different temperatures, the strong coupling between the $4f$ and itinerant electrons has been pointed out, which will be responsible for the interesting and complicated magnetic properties observed in $\text{Eu}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ where the A-type magnetic structure changes to the A-type canted AFM structure at intermediate Co doping levels around $x \approx 0.1$, and then to the ferromagnetic order along the c axis at $x \approx 0.18$ [9].

The importance of the magnetic interaction between Eu $4f$ electrons and itinerant d electrons has also been pointed out

in an Eu-based filled skutterudite compound $\text{EuFe}_4\text{As}_{12}$ [11]. However, the magnetism of $\text{EuFe}_4\text{As}_{12}$ can be quite different from the aforementioned $\text{Eu}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$. $\text{EuFe}_4\text{As}_{12}$ exhibits a magnetic phase transition at $T_C \approx 152$ K where both Eu $4f$ and itinerant Fe moments order at the same time [11,12]. It is pointed out that the transition temperature of $T_C \approx 152$ K is relatively high in comparison with other related compounds [11]. When Fe is replaced by Ru or Os, the magnetic ordering temperature is suppressed to 25 K for $\text{EuOs}_4\text{As}_{12}$ and no magnetic order is observed down to 2 K in $\text{EuRu}_4\text{As}_{12}$ [11]. On the other hand, when Eu^{2+} is replaced by other divalent Sr or Ba ions, no magnetic order is observed although ferromagnetic spin fluctuations were reported [13–15]. In the case of La for the replacement, an itinerant ferromagnetism associated with Fe $3d$ moments is observed below a Curie temperature of ≈ 5.2 K in $\text{LaFe}_4\text{As}_{12}$ [16,17]. The difference of the magnetic ordering temperature for those compounds indicates the strong exchange coupling between Eu $4f$ electrons and itinerant Fe $3d$ electrons [11]. Such strong exchange couplings have also been reported in similar Eu-containing iron skutterudite compounds $\text{EuFe}_4\text{Sb}_{12}$ ($T_C = 85 \pm 4$ K) [18–22] and $\text{EuFe}_4\text{P}_{12}$ ($T_C = 100 \pm 3$ K) [23,24].

As for the spin structure of the magnetic state, magnetic susceptibility $\chi(T)$ measurements on $\text{EuFe}_4\text{As}_{12}$ suggest either a canted ferromagnetic or ferrimagnetic structure below T_C [11]. The effective moment and Curie-Weiss temperature in the paramagnetic state estimated from $\chi(T)$ measurement are reported to be $6.93 \mu_B/\text{f.u.}$ and 46 K, respectively. The value of the effective moments is slightly smaller than that expected for divalent Eu^{2+} ($S = 7/2$) of $\mu_{\text{eff}} = 7.94 \mu_B$ [11]. The magnetic field dependence of magnetization at 2 K for

$\text{EuFe}_4\text{As}_{12}$ shows a saturation moment of $4.5 \mu_B/\text{f.u.}$ at 1 T, which is much smaller than $7 \mu_B$ expected for Eu^{2+} [11]. Similar magnetic properties have been reported in the isostructural compound $\text{EuFe}_4\text{Sb}_{12}$ which was initially considered as a ferromagnet below T_C [18–20]. Later on, the x-ray magnetic circular dichroism spectroscopy (XMCD) and x-ray absorption spectroscopy (XAS) measurements suggest a ferrimagnetic state in $\text{EuFe}_4\text{Sb}_{12}$ where ferromagnetically aligned Eu spins are ordered antiferromagnetically with ordered Fe moments [25], however, the possibility of a canted ferromagnetic state was not fully ruled out. In the case of $\text{EuFe}_4\text{As}_{12}$, such measurements have not been performed yet. Therefore, the detailed studies of the local magnetic and electronic properties of the magnetic ions are important to reveal the magnetic structure as well as the magnetic properties of the system.

Nuclear magnetic resonance (NMR) is a powerful technique to investigate the magnetic properties of materials from a microscopic point of view. In particular, one can obtain direct and local information of magnetic state at nuclear sites, helping to determine the magnetic structure of magnetic systems. Although the magnetic state of the Eu ions in $\text{EuFe}_4\text{As}_{12}$ is a key to understand the magnetic properties of the system, there have been no Eu NMR studies of this compound up to now to our knowledge.

In this paper, we have carried out ^{153}Eu NMR and ^{75}As nuclear quadrupole resonance (NQR) measurements to investigate the magnetic properties of $\text{EuFe}_4\text{As}_{12}$, especially focusing on the magnetic state of the Eu ions, from a microscopic point of view. From the external magnetic field dependence of ^{153}Eu NMR spectrum, the Eu ions are shown to be in divalent state with nearly $7 \mu_B$, which ordered ferromagnetically without any canting component, revealing a ferrimagnetic ordered state in $\text{EuFe}_4\text{As}_{12}$. We also report the local distortion at the Eu site from the cubic symmetry in the magnetically ordered state, which will be important to understand the physics of motion for Eu ions called rattling in the cage formed by $\text{Fe}_4\text{As}_{12}$ units.

II. EXPERIMENTAL

Polycrystalline $\text{EuFe}_4\text{As}_{12}$ samples were prepared at high temperature and high pressures using a wedge-type cubic anvil high-pressure apparatus [11]. The chemical composition of the samples was determined by energy-dispersive x-ray spectroscopy (EDS) measurements using a JEOL scanning electron microscope and was found to be $\text{Eu}_{1.06}\text{Fe}_{4.00}\text{As}_{12.2}$ showing no obvious deficiency of Eu ions. Good chemical homogeneity was found in the powder samples. The crystal structure of the sample was characterized by powder x-ray diffraction (XRD) using $\text{Mo } K_\alpha$ radiation and silicon as a standard. The powder samples are loosely packed into a sample case, which allows the crystallites to be oriented along the applied magnetic field direction.

NQR measurements of ^{75}As ($I = \frac{3}{2}$, $\frac{\gamma_N}{2\pi} = 7.2919 \text{ MHz/T}$, $Q = 0.29$ barns) and NMR measurements of ^{153}Eu ($I = \frac{5}{2}$, $\frac{\gamma_N}{2\pi} = 4.632 \text{ MHz/T}$, $Q = 2.49$ barns) nuclei were conducted using a homemade phase-coherent spin-echo pulse spectrometer. ^{153}Eu NMR spectra in zero and nonzero magnetic fields H in the magnetically ordered state and ^{75}As -NQR spectra

were measured in steps of frequency f by measuring the intensity of the Hahn spin echo. The ^{75}As and ^{153}Eu nuclear spin-lattice relaxation rate $1/T_1$ was measured with a saturation recovery method. $1/T_1$ at each temperature was determined by fitting the nuclear magnetization M versus time t using the exponential function $1 - M(t)/M(\infty) = e^{-(3t/T_1)}$ for ^{75}As NQR, and $1 - M(t)/M(\infty) = 0.029e^{-(t/T_1)} + 0.18e^{-(6t/T_1)} + 0.79e^{-(15t/T_1)}$ for ^{153}Eu NMR, where $M(t)$ and $M(\infty)$ are the nuclear magnetization at time t after the saturation and the equilibrium nuclear magnetization at $t \rightarrow \infty$, respectively.

III. RESULTS AND DISCUSSION

A. ^{153}Eu zero field NMR in the ferrimagnetic state

Figure 1 shows the frequency-swept ^{153}Eu NMR spectrum in zero magnetic field at 4.3 K in the magnetically ordered state. The observation of the ^{153}Eu NMR signals clearly evidences that the magnetic moments of Eu 4f electrons order in

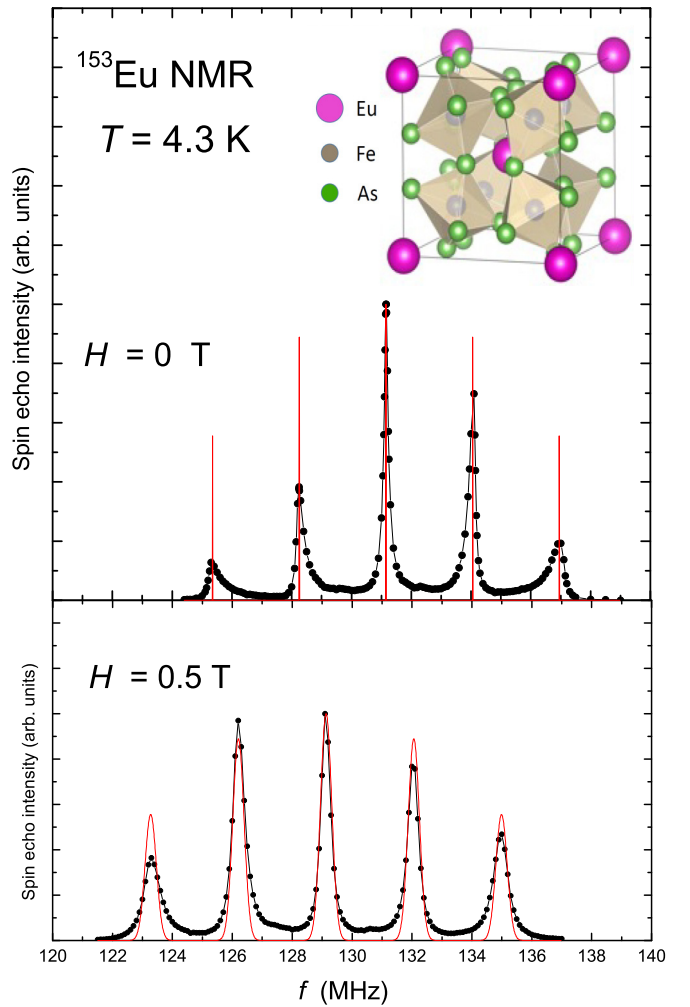


FIG. 1. Top: ^{153}Eu -NMR spectrum in zero magnetic field at $T = 4.3 \text{ K}$ in the magnetic ordering state. The lines are the calculated positions of ^{153}Eu -NMR spectrum using $B_{\text{int}} = -28.14 \text{ T}$ and $\nu_Q = 2.90 \text{ MHz}$. The inset shows the crystal structure. Bottom: ^{153}Eu -NMR spectrum under $H = 0.5 \text{ T}$. The curves are calculated spectrum using the same parameters where a line broadening of 0.35 MHz is introduced for each line.

TABLE I. B_{int} and ν_Q from ^{153}Eu NMR measurements at 4.2 K for $\text{EuFe}_4\text{As}_{12}$, the helical antiferromagnets (AFM) EuCo_2P_2 and EuCo_2As_2 , and the A-type antiferromagnet EuGa_4 and the magnetic moments of Eu ions M_{Eu} from neutron diffraction measurements on EuCo_2P_2 [31] and EuCo_2As_2 [32].

	B_{int} (T)	ν_Q (MHz)	M_{Eu} (μ_B)	Ground state (ordered temperature)	Ref.
$\text{EuFe}_4\text{As}_{12}$	-28.14(5) T	2.90(5)		Ferrimagnet ($T_C = 154$ K)	This work
EuCo_2P_2	-27.5(1) T	30.6(1)	7.26	Helical AFM ($T_N = 45$ K)	[28]
EuCo_2As_2	-25.75(2) T	30.2(2)	6.9(1)	Helical AFM ($T_N = 66.5$ K)	[29]
EuGa_4	-27.08 T	30.5		A-type AFM ($T_N = 16$ K)	[30]

the magnetic state. The relatively sharp peaks in the observed spectrum indicate a high quality of the powder samples. The peak positions of the spectrum are well explained by the combination of a large Zeeman interaction due to magnetic field [for the present case, an internal magnetic induction (B_{int}) at the Eu site] and a small quadrupole interaction whose nuclear spin Hamiltonian is given as follows;

$$\mathcal{H} = -\gamma_n \hbar \mathbf{I} \cdot \mathbf{B}_{\text{int}} + \frac{h\nu_Q}{6} \left[3I_z^2 - I^2 + \frac{1}{2}\eta(I_+^2 + I_-^2) \right], \quad (1)$$

where

$$I_z = \frac{1}{2}(I_+ e^{-i\phi} + I_- e^{i\phi}) \sin\theta + I_z \cos\theta. \quad (2)$$

Here h is Planck's constant, and ν_Q is nuclear quadrupole frequency defined by $\nu_Q = 3e^2QV_{ZZ}/2I(2I-1)\hbar$ ($= 3e^2QV_{ZZ}/20\hbar$ for $I = 5/2$) where Q is the electric quadrupole moment of the Eu nucleus, V_{ZZ} is the electric field gradient (EFG) at the Eu site in the coordinate of the principal X , Y , and Z axes of EFG, and η is the asymmetry parameter of the EFG [26]. θ and ϕ are the polar and azimuthal angles between the Z axis of EFG and the direction of B_{int} , respectively, where the quantization axis (z axis) for the Zeeman interaction is pointing along the B_{int} direction.

In the case of $I = 5/2$, when $\eta = 0$, the NMR spectrum is composed of a central transition line ($I_z = 1/2 \leftrightarrow -1/2$) and two pairs of satellite lines shifted from the central transition line by $\pm \frac{1}{2}\nu_Q(3\cos^2\theta - 1)$ (for the transitions of $I_z = 3/2 \leftrightarrow 1/2$ and $-3/2 \leftrightarrow -1/2$), and $\pm\nu_Q(3\cos^2\theta - 1)$ (for $I_z = 5/2 \leftrightarrow 3/2$ and $-5/2 \leftrightarrow -3/2$). The five solid lines shown in Fig. 1 are the calculated positions using $|B_{\text{int}}| = 28.14(5)$ T, $\nu_Q = 2.90(5)$ MHz, $\eta = 0$ and $\theta = 0^\circ$ (and, thus, $\phi = 0^\circ$), which reproduce the observed positions very well. Since B_{int} mainly originates from core polarization from $4f$ electrons and is oriented in a direction opposite to that of the Eu spin moments, the sign of B_{int} is considered to be negative [27]. The observed $B_{\text{int}} = -28.14(5)$ T is close to the values of B_{int} reported from ^{153}Eu zero-field NMR in the helical antiferromagnets EuCo_2P_2 [28] and EuCo_2As_2 [29], and the A-type antiferromagnet EuGa_4 [30] as shown in Table I. The values of Eu magnetic moments in EuCo_2P_2 and EuCo_2As_2 determined by neutron diffraction measurements are close to $7 \mu_B$ expected for Eu^{2+} ion ($S = 7/2$) [31,32]. Since the Eu ordered moment M_{Eu} is proportional to $|B_{\text{int}}/A_{\text{hf}}|$ where A_{hf} is the hyperfine coupling constant mainly originating from the core polarization, the similar value of $B_{\text{int}} = -28.14(5)$ T in $\text{EuFe}_4\text{As}_{12}$ in comparison with those in other Eu compounds leads to the conclusion that the Eu ions are in Eu^{2+} state with $S = 7/2$.

It is noted that, from the XRD measurements [11], $\text{EuFe}_4\text{As}_{12}$ crystallizes in a body-centered cubic structure (the space group $Im\bar{3}$, see the inset of Fig. 1 [33]) with a lattice constant of 8.3374 \AA at room temperature. Since the local symmetry of the Eu site is cubic in the structure (T_h), one expects no quadrupole interaction because the EFG due to the charges on the neighboring ions is zero. In general, there is another contribution to the EFG at the Eu site originating from the on-site f electrons. However, this EFG contribution is also zero because of the spherical charge distribution of $4f^7$ electrons for Eu^{2+} ions with zero angular momentum $L = 0$, which is independent of crystal structure. Therefore, the finite quadrupole interaction at the Eu site observed in the magnetically ordered state must be attributed to the contribution from the neighboring ions. Thus, the experimental data clearly evidence the lowering symmetry at the Eu site from cubic. We will discuss this issue later.

The direction of B_{int} from the NMR spectrum is not determined in the present case. Usually, one can determine the direction from the value of θ if we know the principal axis of the EFG. However, as described above, our NMR spectrum indicates that the local symmetry at the Eu site in the magnetically ordered state is different from what is expected from the high-temperature cubic one. Therefore, the EFG direction cannot be determined, making the determination of the direction for B_{int} impossible at present.

It is also important to point out that the satellite lines of the observed ^{153}Eu zero-field NMR are asymmetric and are tailing toward to the central transition line. This asymmetric shape is reminiscent of a so-called powder pattern of NMR spectrum. Although, in general, we do not expect the powder-pattern-like shape in zero-field NMR spectrum, we have the following three possibilities: The first one is due to the distribution of ν_Q , the second one comes from the slight distribution of θ , and the last one originates from domain walls. The first scenario has been used to explain the similar asymmetric ^{153}Eu zero-field NMR lines observed in EuGa_4 where a log-normal distribution of ν_Q was used [30]. However, we do not find such large distribution of ν_Q in our case, as will be shown below. As for the second scenario, as the small deviation in θ from 0 degree makes the satellite line shift toward the central transition line as described in the above equations for the satellite line positions, one may explain the characteristic asymmetric shape of the satellite lines by taking the small deviation from $\theta = 0^\circ$ into consideration. In fact, such scenario has been applied to explain the asymmetric lines observed in EuAl_4 where the distribution of θ is estimated to be at most 6° or less [34]. However, for our case, this seems to be not the case. Since the signal intensity does not go down

to zero between the satellite lines, to reproduce the spectrum, one needs to have a relatively large distribution of θ up to at least $\approx 20^\circ$, which seems to be too large. In contrast, the third scenario can be the main reason for the observed asymmetric shape since the asymmetric shape of the lines becomes more symmetric when magnetic field is applied (a typical spectrum measured at $H = 0.5$ T is shown at the bottom of Fig. 1). The red curves in the figure are the calculated spectrum at $H = 0.5$ T with the same values of B_{int} and ν_Q where we assume a line broadening of 0.35 MHz for each line. It is noted that, in a magnetic field of 0.5 T, the values of line width (full width at half maximum, $FWHM \approx 0.4\text{--}0.5$ MHz) for each line are nearly the same, as the calculated spectrum reproduces the observed spectrum very well. This indicates that the broadening of each line originates from the slight distribution of B_{int} (less than $\approx 0.4\%$) and the effect of the distribution in ν_Q into the line width is almost negligible. It is known that the deviation of rare-earth filling factor from unity in filled skutteruride compounds produces the distribution of ν_Q and thus broadening of spectrum at the rare-earth site [35–37]. Therefore, the negligible small distribution of ν_Q in $\text{EuFe}_4\text{As}_{12}$ suggests that the Eu filling factor is close to unity, which is consistent with the results of the EDS measurements, confirming again the high quality of our samples.

B. Magnetic field dependence of ^{153}Eu NMR spectrum

In order to gain more insight into the magnetic properties of $\text{EuFe}_4\text{As}_{12}$, especially the Eu ordered moments in the magnetically ordered state, we have measured ^{153}Eu NMR spectrum using the loosely packed sample under an external magnetic field H . Figure 2(a) shows the magnetic field dependence of the ^{153}Eu NMR spectrum at 4.3 K. The spectrum shifts to lower frequency as magnetic field increases. At the same time, as discussed above, the asymmetric shape of the satellite lines become more symmetric under magnetic field, indicating the main reason for the asymmetry can be due to domain walls where the Eu ordered moments change the direction making the distribution of θ . It is also noted that the spacings between the lines keep constant, indicating θ does not change with the application of magnetic field. Given the total magnetization saturates around 1 T at $T = 2$ K as shown in the inset of Fig. 2(b), these results indicate that most of the small particles are aligned along the magnetic field direction. This means there must be a finite magnetic anisotropy in the magnetic ordered state, although we cannot estimate the magnitude of it.

The magnetic field dependence of the resonance frequency for the central line (f_c) is shown in Fig. 2(b) and the slope of the H dependence of f_c is found to be -4.63 MHz/T which is exactly the same as $-\gamma/2\pi$ of ^{153}Eu nucleus. Since the effective field at the Eu site is given by the vector sum of B_{int} and H , i.e., $|B_{\text{eff}}| = |B_{\text{int}} + H|$, the resonance frequency is expressed as $f = \gamma/2\pi |B_{\text{eff}}|$. Therefore, the value of the slope clearly indicates that the direction of B_{int} is antiparallel to that of H and also that all Eu ordered moments align along H without any appreciable deviation. Thus, one can conclude that the ferromagnetically aligned Eu ordered moments do not have any canting components up to 8 T, excluding clearly a canted ferromagnetic state as a possible ground state. To

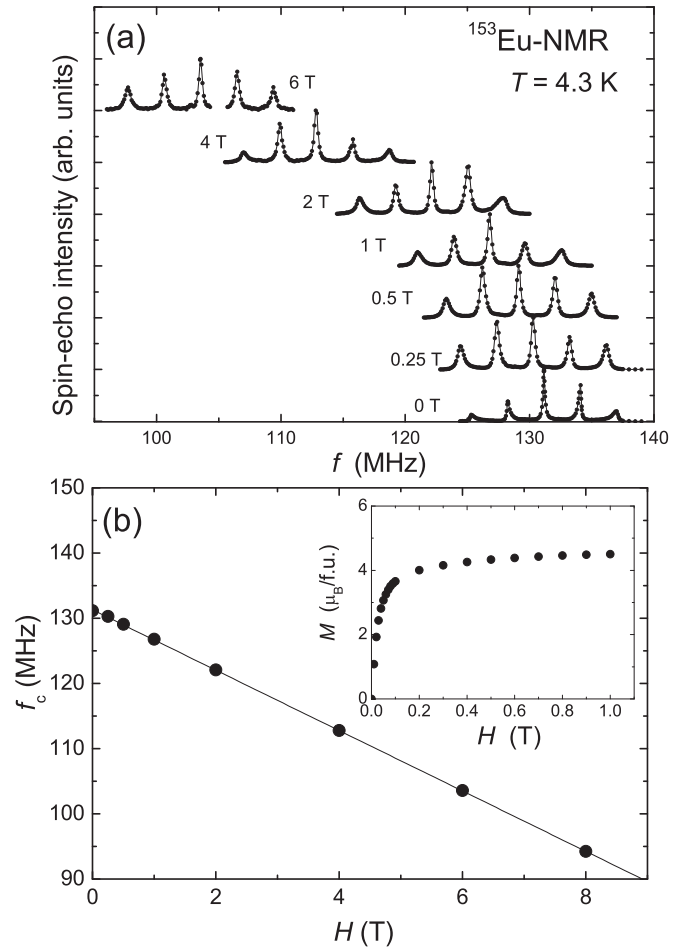


FIG. 2. (a) Field dependence of ^{153}Eu -NMR spectrum at 4.3 K. (b) Field dependence of ^{153}Eu -NMR central line frequency (f_c) at 4.3 K. The solid line is a linear fit whose slope is exactly same as $-\gamma/2\pi$ of ^{153}Eu nucleus. The inset shows the field dependence of magnetization measured at 2 K.

explain the saturated magnetic moment of $4.5 \mu_B/\text{f.u.}$ in the magnetic ordering state [see the inset of Fig. 2(b)], the Fe 3d electrons must be magnetically ordered in antiparallel direction with respect to the Eu^{2+} ordered moments, producing the ferrimagnetic ground state. Since the Eu ordered moments are estimated to be $\approx 7 \mu_B$ from the magnitude of B_{int} as discussed above, the Fe 3d ordered moments are estimated to be $\approx 0.6 \mu_B$ for each Fe ion. A similar ferrimagnetic state has also been reported in the isostructural compound $\text{EuFe}_4\text{Sb}_{12}$ by XMCD and XAS measurements [25]. The ferrimagnetic state is consistent with the results from density function theory based calculations for $\text{EuFe}_4\text{As}_{12}$ [38] as well as other similar compounds such as $\text{EuFe}_4\text{P}_{12}$ [39] and $\text{EuFe}_4\text{Sb}_{12}$ [40].

C. Temperature dependence of ^{153}Eu zero-field NMR

Figure 3(a) shows the temperature dependence of ^{153}Eu zero-field NMR spectra, where the spectra shift to lower frequency with increasing temperature. This is due to the reduction of $|B_{\text{int}}|$, which decreases from 28.14 T at 4.3 K to 21.19 T at 90 K. The red squares shown in Fig. 3(b) exhibit the temperature dependence of $|B_{\text{int}}|$. In the figure, we also

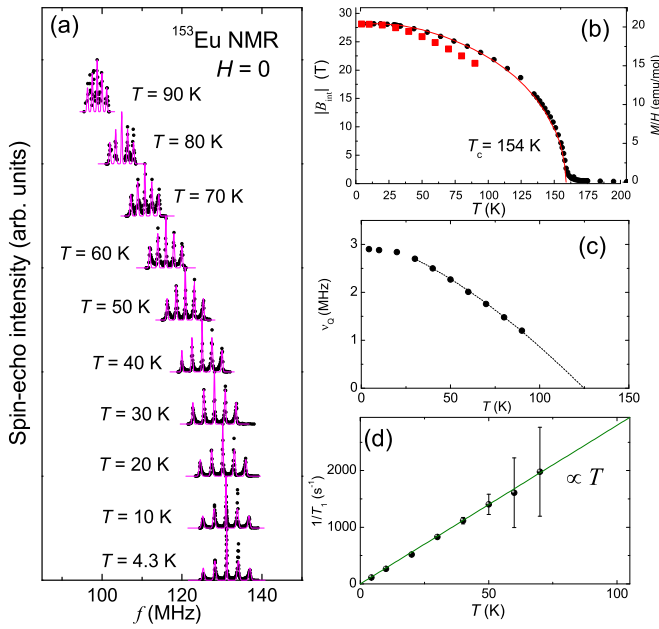


FIG. 3. (a) Temperature dependence of ^{153}Eu -NMR spectrum under zero magnetic field in the magnetic ordering state. The curves are the calculated ^{153}Eu -NMR spectra. (b) Temperature dependence of $|B_{\text{int}}|$. The black circles show the temperature dependence of M/H measured at $H = 0.1$ T reported previously [11]. The red curve is the Brillouin function with $J = S = 7/2$ and $T_C = 154$ K. (c) Temperature dependence of ν_Q at the ^{153}Eu site. (d) Temperature dependence of ^{153}Eu $1/T_1$ under zero magnetic field. The straight line shows the Korringa relation $1/T_1 T = 28$ (sK) $^{-1}$.

plotted the M/H data measured at 0.1 T by black circles [11]. As shown by the red curve, the temperature dependence of M/H is well reproduced by the Brillouin function, which was calculated based on the Weiss molecular field model with $J = S = 7/2$ and $T_C = 154$ K. This suggests that, although both the Eu and Fe ordered moments contribute to the total magnetization, the temperature dependence of M/H can be mainly characterized by the properties of Eu ordered moments. In addition, the results indicate that the Eu ordered moments are well described by a local moment picture even in a metallic state as revealed by the resistivity measurements [11,12] as well as nuclear relaxation measurements described below. As shown in Fig. 3(b), on the other hand, the temperature dependence of $|B_{\text{int}}|$ slightly deviates from that of M/H . As $|B_{\text{int}}|$ is proportional to $A_{\text{hf}} M_{\text{Eu}}$, $|B_{\text{int}}|$ should scale with M/H since its temperature dependence is well explained by the $S = 7/2$ local moment picture. Although the reason for the deviation is not clear at present, it may be due to the local distortion at the Eu site in the ferrimagnetic state. As described above, the $|B_{\text{int}}|$ is mainly determined by the hyperfine coupling originated from the $4f$ electron core-polarization mechanism, which is atomic in nature. Therefore, the hyperfine coupling constant will not be affected by the local environment at the Eu site. On the other hand, if one considers the effects of the transferred hyperfine field $B_{\text{int}}^{\text{trans}}$ at the Eu site from the nearest-neighbor Fe ordered moments, the $B_{\text{int}}^{\text{trans}}$ can be affected by the local distortion at the Eu site since the transferred hyperfine field largely depends on

the strength of Fe-As-Eu covalent bond. Although we cannot conclude the origin of the deviation, it would be interesting if it originates from the effects of $B_{\text{int}}^{\text{trans}}$ since this may be experimental evidence showing the coupling between the $3d$ electrons of Fe and the $4f$ electrons of Eu in $\text{EuFe}_4\text{As}_{12}$.

The temperature dependence of ν_Q at the ^{153}Eu site is shown in Fig. 3(c) where ν_Q decreases from 2.90 MHz at 4.3 K to 1.2 MHz at 90 K. Such a huge reduction of ν_Q by $\approx 59\%$ cannot be explained by thermal lattice expansion [41], which is normally described by an empirical relation $\nu_Q(T) = \nu_Q(0)(1 - \alpha_Q T^{3/2})$ with a fitting parameter α_Q . As described above, one does not expect the finite value of ν_Q at the Eu site in the high-temperature body-centered cubic structure. In fact, ν_Q seems to disappear around $T \approx 125$ K estimated from the smooth extrapolation using the experimental data at $T = 30$ –90 K, and ν_Q will be zero in the paramagnetic state above $T_C = 154$ K where the cubic structure ($Im\bar{3}$) was determined by the XRD measurements at room temperature [11].

Since the finite values of ν_Q reflecting the degree of the local distortion of the cubic symmetry at the Eu site suggest a structural phase transition, we have carried out XRD measurements in the temperature range of $T = 113$ –300 K. We did not observe clear evidence for structural phase transition in the XRD patterns down to 113 K, which is the lowest temperature we can achieve by using our XRD spectrometer with a nitrogen gas flow type cryostat. Although the results may suggest no structural phase transition at least down to 113 K, this does not fully rule out the possibility in the compound. One of the possibilities is that the lowest temperature of 113 K may not be low enough to detect the structural phase transition, which could occur at T_C estimated from the temperature dependence of ν_Q . The situation here could be similar to the electron diffraction measurements of the skutterudite compound $\text{PrRu}_4\text{P}_{12}$ where the superlattice spots due to the structural phase transition were clearly observed at 12 K, however, the intensity of the superlattice spots becomes very weak at 40 K even though the structural transition temperature is around 60 K [42]. Another possibility is that ordinary XRD measurements using powder samples may not be able to detect the structural phase transition. This has also been reported in $\text{PrRu}_4\text{P}_{12}$ where only synchrotron radiation XRD measurements using single crystals revealed a structural phase transition [43,44]. The structural phase transition was reported to change only in the space group (from $Im\bar{3}$ for the high-temperature phase to $Pm\bar{3}$ for the low-temperature phase) while the cubic crystal symmetry of structure is unchanged [42–44]. It is interesting to point out that, even in the cubic symmetry, the slight displacements of P and Fe atoms have been reported in the low-temperature phase of $\text{PrRu}_4\text{P}_{12}$ [42–44]. Such displacement may produce the local distortion of the cubic symmetry at the rare-earth sites, giving rise to the finite EFG. This could explain our results in $\text{EuFe}_4\text{As}_{12}$, of course, we cannot conclude it though. Thus, it is important to carry out the low-temperature XRD measurements, especially using single crystals if available, to clarify whether or not the crystal structure in the magnetically ordered state is different from the high-temperature one. Such experiments are highly called for.

From the behavior of the temperature dependence of ν_Q , we consider that the structural phase transition would be a second-order type of phase transition if the local distortion at the Eu sites were due to a structural phase transition. Since the specific heat measurements do not show any anomaly other than at T_C [12], one may speculate that the magnetic ordering takes place with a possible concomitant structural phase transition, although the estimated $T \approx 125$ K is a little bit far from $T_C = 154$ K.

It is also interesting to point out that the specific heat measurements [12] suggest that the rattling motion of the Eu atoms is not prominent in $\text{EuFe}_4\text{As}_{12}$. This has been generally explained in terms of the ionic radius of Eu^{2+} ions greater than those of trivalent rare-earth ions, which gives rise to a less space for the rattling motion of the Eu^{2+} ions in the $\text{Fe}_4\text{As}_{12}$ cage. However, as the cubic electric field at the rare-earth site is also considered to be one of the keys for the rattling motion, the lowering of the cubic symmetry at the Eu site in $\text{EuFe}_4\text{As}_{12}$ may result in restricting the rattling motion of the Eu atoms. Even from this point of view, as described above, further detailed studies on the crystal structure at low temperatures are requested, which may provide further insights into the rattling physics in filled skutterudite compounds.

At the end of this section, we show the temperature dependence of $1/T_1$ measured at the central line of the ^{153}Eu zero-field NMR spectrum. As shown in Fig. 3(d), $1/T_1$ is proportional to temperature, obeying a Korringa law $1/T_1 T = 28$ (sK) $^{-1}$ expected for a metallic state. This result confirms the metallic ground state in the ferrimagnetic state from a microscopic point of view, consistent with the resistivity measurements [11,12].

D. ^{75}As NQR in the paramagnetic state

Figure 4(a) shows the temperature dependence of the ^{75}As NQR spectrum from 160–300 K in the paramagnetic state. In NQR spectrum under zero magnetic field for ^{75}As nuclei with $I = 3/2$, one expects a single transition line at a frequency of $\nu_{\text{NQR}} = \nu_Q \sqrt{1 + \eta^2/3}$. The observed lines are sharp with the nearly temperature-independent line width ($\text{FWHM} \approx 65$ kHz), which is smaller than $\text{FWHM} \approx 140$ kHz and is greater than ≈ 33 kHz for high-quality samples of $\text{SrFe}_4\text{As}_{12}$ [15] and $\text{LaFe}_4\text{As}_{12}$ [45], respectively, but is much smaller than ≈ 400 kHz in $\text{SrOs}_4\text{As}_{12}$ having a lesser degree of homogeneity of crystals [46]. This indicates again the high quality of the samples and also the Eu filling factor close to unity. As shown in the figure, the peak position slightly shifts to lower frequency with increasing temperature without showing any sudden changes, indicating that there is no structural anomaly in the paramagnetic state of $\text{EuFe}_4\text{As}_{12}$. On the other hand, below T_C , the spectrum becomes broader and the signal intensity decreases. Although we could not measure the spectrum around T_C because of the poor signal intensity due to the shortening of nuclear spin-spin relaxation time T_2 originating from the phase transition, we were able to measure the spectrum at $T = 90$ K. The very broad spectrum with the two-peak structure is observed as shown in the inset of Fig. 4(a) where we also plot the spectrum ($T = 160$ K) observed in the paramagnetic state for comparison.

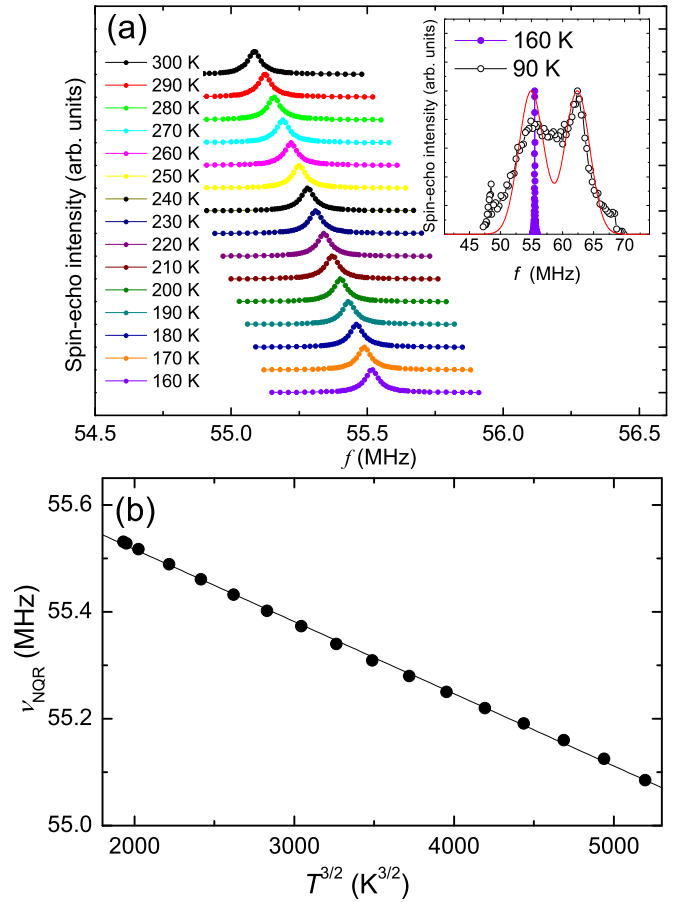


FIG. 4. (a) Temperature dependence of the ^{75}As -NQR spectrum for $\text{EuFe}_4\text{As}_{12}$ in the paramagnetic state. The inset shows a typical ^{75}As -NQR spectrum measured at $T = 90$ K in the magnetically ordered state. The red curve is a calculated result with $\nu_{\text{NQR}} = 58.7$ MHz and $|B_{\text{int}}| = 5.1$ kOe at the As site. (b) Temperature dependence of ^{75}As -NQR frequency ν_{NQR} in the paramagnetic state as a function of $T^{3/2}$. The solid line is the fitting result (see text).

One possible explanation of the two-peak structure is to introduce an internal field at the As site from the Eu and Fe ordered moments in the ferrimagnetic state. It is also important to point out that the center of mass of the spectrum shifts to higher frequency, indicative of an increase of ν_{NQR} . Based on this consideration, we have calculated ^{75}As NQR spectrum assuming $|B_{\text{int}}| = 5.1$ kOe and $\nu_{\text{NQR}} = 58.7$ MHz with a line broadening of 4 MHz. The red curve is the calculated spectrum, which seems to capture the characteristic shape of the spectrum. Although we cannot determine the direction of $|B_{\text{int}}|$ as well as its sign, the large change of ν_{NQR} from 55.5–55.1 MHz in the paramagnetic state to 58.7 MHz at 90 K would be consistent with the observation of the local distortion related to a possible structural phase transition suggested by the ^{153}Eu NMR measurements.

The temperature dependence of ν_{NQR} determined from the peak positions of the NQR spectra is shown in Fig. 4(b). Similar temperature dependences of ν_{NQR} have been observed in $\text{SrFe}_4\text{As}_{12}$ [15], $\text{SrOs}_4\text{As}_{12}$ [46] and also in other filled skutterudite compounds [45,47–51] where the temperature dependence is found to obey an empirical relation $\nu_{\text{NQR}}(T) =$

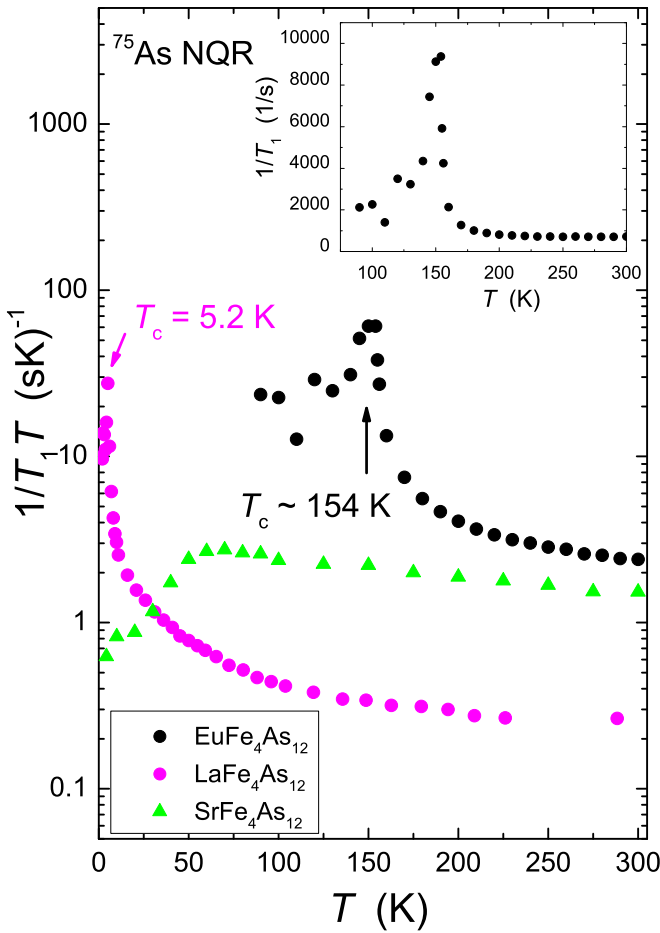


FIG. 5. Temperature dependence of ^{75}As $1/T_1T$ in $\text{EuFe}_4\text{As}_{12}$ (black circles), together with those in $\text{LaFe}_4\text{As}_{12}$ (magenta circles) from Ref. [52] and $\text{SrFe}_4\text{As}_{12}$ (green triangles) from Ref. [15]. The inset shows the temperature dependence of $1/T_1$.

$\nu_{\text{NQR}}(0)(1 - \alpha_Q T^{3/2})$ with a fitting parameter α_Q [41]. As shown by the curve in Fig. 4(b), the temperature dependence of ν_{NQR} at As sites in $\text{EuFe}_4\text{As}_{12}$ also follows the relation with $\alpha_Q = 2.24 \times 10^{-6} \text{ K}^{-3/2}$. The value of $\alpha_Q = 2.24 \times 10^{-6} \text{ K}^{-3/2}$ is similar to the values for $\text{SrFe}_4\text{As}_{12}$ ($3.21 \times 10^{-6} \text{ K}^{-3/2}$) [15] and $\text{SrOs}_4\text{As}_{12}$ ($2.09 \times 10^{-6} \text{ K}^{-3/2}$) [46].

It is noted that one cannot determine the values of ν_Q and η for the As nuclei separately from only the NQR spectrum measurements. The values of $\eta = 0.4\text{--}0.45$ have been reported in the isostructural compounds $\text{SrM}_4\text{As}_{12}$ ($M = \text{Fe}, \text{Os}$) [15,46]. Since the crystal structure of $\text{EuFe}_4\text{As}_{12}$ in the paramagnetic state is the same with those compounds, we expect the similar value of η in the present compound.

To investigate the magnetic fluctuations in the paramagnetic state in $\text{EuFe}_4\text{As}_{12}$, we have measured the temperature dependence of ^{75}As spin-lattice relaxation rate $1/T_1$ in zero magnetic field. Figure 5 shows the temperature dependence of $1/T_1T$. For comparison, we also plotted the $1/T_1T$ data for the itinerant ferromagnet $\text{LaFe}_4\text{As}_{12}$ reported previously [52] where a clear peak in $1/T_1T$ can be observed at a Curie temperature of 5.2 K. With decreasing temperature, $1/T_1T$ for $\text{EuFe}_4\text{As}_{12}$ increases gradually and shows a divergent

behavior around 153 K, corresponding to the ferrimagnetic phase transition at $T_C \approx 154 \text{ K}$. The values of $1/T_1T$ for $\text{EuFe}_4\text{As}_{12}$ above T_C are almost one order of magnitude greater than those in $\text{LaFe}_4\text{As}_{12}$ at the temperature region. Since there is no 4f electrons in $\text{LaFe}_4\text{As}_{12}$, the largely enhanced ^{75}As relaxation in $\text{EuFe}_4\text{As}_{12}$ could mainly originate from the fluctuations of the Eu 4f electron moments. According to Moriya [53], when the magnetic fluctuations are dominated by the paramagnetic fluctuations of local moments, $1/T_1$ is expected to be a constant well above magnetic ordering temperature. As shown in the inset of Fig. 5, $1/T_1$ is nearly independent of temperature at high temperatures. This indicates that the magnetic fluctuations in the paramagnetic state of $\text{EuFe}_4\text{As}_{12}$ are characterized by the fluctuations of the local moment nature of the Eu 4f electron spins. This is consistent with the local moment picture of the Eu spins indicated by the temperature dependence of M/H discussed above.

It is also interesting to compare the $1/T_1T$ data for $\text{LaFe}_4\text{As}_{12}$ with those for the paramagnetic metal $\text{SrFe}_4\text{As}_{12}$ (plotted by the green triangles in Fig. 5) where the existence of ferromagnetic spin fluctuations was reported [46]. The values of $1/T_1T$ of $\text{LaFe}_4\text{As}_{12}$ well above $T_C = 5.2 \text{ K}$ are much less than those in $\text{SrFe}_4\text{As}_{12}$. Although we do not have the detailed information about the local density of states at the As sites for both compounds, it is interesting if such reduction of $1/T_1T$ in $\text{LaFe}_4\text{As}_{12}$ could be attributed to the suppression of ferromagnetic spin fluctuations, resulting in the ferromagnetic order at $T_C = 5.2 \text{ K}$. Further studies, especially electronic structure calculations, are required to address this issue.

IV. SUMMARY

In summary, we performed ^{75}As NQR and ^{153}Eu NMR measurements on the filled skutterudite compound $\text{EuFe}_4\text{As}_{12}$ with $T_C = 154 \text{ K}$. We observed the ^{153}Eu NMR spectrum in the magnetically ordered state, which reveals that the Eu^{2+} ordered moments are close to $7 \mu_B$. From the external magnetic field dependence of ^{153}Eu NMR spectrum observed in the magnetically ordered state, we found that the Eu ordered moments ferromagnetically align the magnetic field direction without any canting component. Taking the magnetization data into consideration, we determined the magnetic ground state of $\text{EuFe}_4\text{As}_{12}$ to be ferrimagnetic in which the Fe 3d moment and the Eu 4f moment are magnetically ordered with antiferromagnetic coupling. The observed ^{153}Eu NMR spectrum shows quadrupole split lines, which are not expected at the Eu site in the cubic structure ($Im\bar{3}$) determined by the XRD measurements at room temperature, suggesting the lowering of the local symmetry at the Eu site at low temperatures. The temperature dependence of ^{75}As $1/T_1T$ suggests that the magnetic fluctuations in the paramagnetic state are dominated by the Eu 4f electron spins, which are well described by the local moment picture. It is shown that ^{153}Eu NMR can be a unique tool in determining the magnetic structure in the Eu compound. It is interesting to study other Eu-based magnetic compounds, such as $\text{EuFe}_4\text{Sb}_{12}$, $\text{EuOs}_4\text{Sb}_{12}$, $\text{EuFe}_4\text{P}_{12}$, and $\text{EuOs}_4\text{P}_{12}$ to gain deeper understanding about the interaction between the d electrons and the Eu 4f electrons.

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- [1] H. Sato, H. Sugawara, Y. Aoki, and H. Harima, Magnetic Properties of Filled Skutterudites, in *Handbook of Magnetic Materials*, edited by K. H. J. Buschow (Elsevier, Amsterdam, 2009), Vol. 18, pp. 1–110, and references therein.
 - [2] G. R. Stewart, *Rev. Mod. Phys.* **56**, 755 (1984).
 - [3] H. B. Radousky, *Magnetism in Heavy Fermion Systems* (World Scientific, Singapore, 2000).
 - [4] K.-H. Müller and V. N. Narozhnyi, *Rep. Prog. Phys.* **64**, 943 (2001).
 - [5] B. C. Sales, Filled skutterudites, in *Handbook on the Physics and Chemistry of the Rare Earths*, edited by K. A. Gschneidner, Jr., J.-C. Bünzli, and V. K. Pecharsky (Elsevier Science, Amsterdam, 2003), Vol. 33, Chap. 211, and references therein.
 - [6] S. Kirchner, S. Paschen, Q. Chen, S. Wirth, D. Feng, J. D. Thompson, and Q. Si, *Rev. Mod. Phys.* **92**, 011002 (2020).
 - [7] H. S. Jeevan, Z. Hossain, D. Kasinathan, H. Rosner, C. Geibel, and P. Gegenwart, *Phys. Rev. B* **78**, 052502 (2008).
 - [8] T. Terashima, M. Kimata, H. Satsukawa, A. Harada, K. Hazama, S. Uji, H. S. Suzuki, T. Matsumoto, and K. Murata, *J. Phys. Soc. Jpn.* **78**, 083701 (2009).
 - [9] W. T. Jin, Y. Xiao, Z. Bukowski, Y. Su, S. Nandi, A. P. Sazonov, M. Meven, O. Zaharko, S. Demirdis, K. Nemkovski, K. Schmalzl, L. M. Tran, Z. Guguchia, E. Feng, Z. Fu, and Th. Brückel, *Phys. Rev. B* **94**, 184513 (2016).
 - [10] S. Zapf and M. Dressel, *Rep. Prog. Phys.* **80**, 016501 (2017).
 - [11] C. Sekine, K. Akahira, K. Ito, and T. Yagi, *J. Phys. Soc. Jpn.* **78**, 093707 (2009).
 - [12] C. Sekine, K. Ito, K. Akihara, Y. Kawamura, Y. Q. Chen, H. Gotou, and K. Matsuhira, *J. Phys.: Conf. Ser.* **592**, 012032 (2015).
 - [13] C. Sekine, T. Ishizaka, K. Nishine, Y. Kawamura, J. Hayashi, K. Takeda, H. Gotou, and Z. Hiroi, *Phys. Procedia* **75**, 383 (2015).
 - [14] K. Nishine, Y. Kawamura, J. Hayashi, and C. Sekine, *Jpn. J. Appl. Phys.* **56**, 05FB01 (2017).
 - [15] Q.-P. Ding, K. Rana, K. Nishine, Y. Kawamura, J. Hayashi, C. Sekine, and Y. Furukawa, *Phys. Rev. B* **98**, 155149 (2018).
 - [16] S. Tatsuoka, H. Sato, K. Tanaka, M. Ueda, D. Kikuchi, H. Aoki, T. Ikeno, K. Kuwahara, Y. Aoki, H. Sugawara, and H. Harima, *J. Phys. Soc. Jpn.* **77**, 033701 (2008).
 - [17] T. Namiki, C. Sekine, K. Matsuhira, M. Wakeshima, and I. Shirotnani, *J. Phys. Soc. Jpn.* **79**, 074714 (2010).
 - [18] M. E. Danebrock, C. B. H. Evers, and W. Jeitschko, *J. Phys. Chem. Solids* **57**, 381 (1996).
 - [19] N. Takeda and M. Ishikawa, *J. Phys. Soc. Jpn.* **69**, 868 (2000).
 - [20] E. Bauer, St. Berger, A. Galatanu, M. Galli, H. Michor, G. Hilscher, Ch. Paul, B. Ni, M. M. Abd-Elmeguid, V. H. Tran, A. Grytsiv, and P. Rogl, *Phys. Rev. B* **63**, 224414 (2001).
 - [21] K. Kihou, I. Shirotnani, Y. Shimaya, C. Sekine, and T. Yagi, *Mater. Res. Bull.* **39**, 317 (2004).
 - [22] E. D. Bauer, A. Slebarski, N. A. Frederick, W. M. Yuhasz, M. B. Maple, D. Cao, F. Bridges, G. Giester, and P. Rogl, *J. Phys.: Condens. Matter* **16**, 5095 (2004).
 - [23] A. Gerard, F. Grandjean, J. A. Hodges, D. J. Braun, and W. Jeitschko, *J. Phys. C* **16**, 2797 (1983).
 - [24] F. Grandjean, A. Gérald, D. J. Braun, and W. Jeitschko, *J. Phys. Chem. Solids* **45**, 877 (1984).
 - [25] V. V. Krishnamurthy, J. C. Lang, D. Haskel, D. J. Keavney, G. Srajer, J. L. Robertson, B. C. Sales, D. G. Mandrus, D. J. Singh, and D. I. Bilc, *Phys. Rev. Lett.* **98**, 126403 (2007).
 - [26] C. P. Slichter, *Principles of Magnetic Resonance*, 3rd ed. (Springer, New York, 1990).
 - [27] A. J. Freeman and R. E. Watson, in *Magnetism*, edited by G. T. Rado and H. Suhl (Academic Press, New York, 1965), Vol. IIA, Ch. 4, pp. 167–305.
 - [28] N. Higa, Q.-P. Ding, M. Yogi, N. S. Sangeetha, M. Hedo, T. Nakama, Y. Ōnuki, D. C. Johnston, and Y. Furukawa, *Phys. Rev. B* **96**, 024405 (2017).
 - [29] Q.-P. Ding, N. Higa, N. S. Sangeetha, D. C. Johnston, and Y. Furukawa, *Phys. Rev. B* **95**, 184404 (2017).
 - [30] M. Yogi, S. Nakamura, N. Higa, H. Niki, Y. Hirose, Y. Ōnuki, and H. Harima, *J. Phys. Soc. Jpn.* **82**, 103701 (2013).
 - [31] M. Reehuis, W. Jeitschko, M. H. Möller, and P. J. Brown, *J. Phys. Chem. Solids* **53**, 687 (1992).
 - [32] X. Tan, G. Fabbri, D. Haskel, A. A. Yaroslavtsev, H. Cao, C. M. Thompson, K. Kovnir, A. P. Menushenkov, R. V. Chernikov, V. O. Garlea, and M. Shatruk, *J. Am. Chem. Soc.* **138**, 2724 (2016).
 - [33] The crystal structure was drawn by using VESTA [K. Momma and F. Izumi, *J. Appl. Crystallogr.* **44**, 1272 (2011)].
 - [34] H. Niki, S. Nakamura, N. Higa, M. Yogi, A. Nakamura, K. Niki, T. Maehira, M. Hedo, T. Nakama, and Y. Ōnuki, *JPS Conf. Proc.* **29**, 012007 (2020).
 - [35] A. Gippius, M. Baenitz, E. Morozova, A. Leithe-Jasper, W. Schnelle, A. Shevelkov, E. Alkaev, A. Rabis, J. A. Mydosh, Y. Grin, and F. Steglich, *J. J. Magn. Magn. Mater.* **300**, e403 (2006).
 - [36] K. Magishi, Y. Nakai, K. Ishida, H. Sugawara, I. Mori, T. Saito, and K. Koyama, *J. Phys. Soc. Jpn.* **75**, 023701 (2006).
 - [37] A. Yamamoto, S. Inemura, S. Wada, K. Ishida, I. Shirotnani, and C. Sekine, *J. Phys.: Condens. Matter* **20**, 195214 (2008).
 - [38] A. Shankar, D. P. Rai, Sandeep, J. Maibam, and R. K. Thapa, *AIP Conf. Proc.* **1661**, 070010 (2015).
 - [39] A. Shankar and R. K. Thapa, *Physica B* **427**, 31 (2013).
 - [40] A. Shankar, D. P. Rai, Sandeep, and R. K. Thapa, *Phys. Procedia* **54**, 127 (2014).
 - [41] S. Takagi, H. Muraoka, T. D. Matsuda, Y. Haga, S. Kambe, R. E. Walstedt, E. Yamamoto, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **73**, 469 (2004).

- [42] C. H. Lee, H. Matsuhata, A. Yamamoto, T. Ohta, H. Takazawa, K. Ueno, C. Sekine, I. Shirotnani, and T. Hirayama, *J. Phys.: Condens. Matter* **13**, L45 (2001).
- [43] C. H. Lee, H. Matsuhata, H. Yamaguchi, C. Sekine, K. Kihou, T. Suzuki, T. Noro, and I. Shirotnani, *Phys. Rev. B* **70**, 153105 (2004).
- [44] C. H. Lee, H. Matsuhata, H. Yamaguchi, C. Sekine, K. Kihou, and I. Shirotnani, *J. Magn. Magn. Mater.* **272–276**, 426 (2004).
- [45] B. Nowak, O. Żogał, A. Pietraszko, R. E. Baumbach, M. B. Maple, and Z. Henkie, *Phys. Rev. B* **79**, 214411 (2009).
- [46] Q.-P. Ding, K. Nishine, Y. Kawamura, J. Hayashi, C. Sekine, and Y. Furukawa, *Phys. Rev. B* **100**, 054516 (2019).
- [47] M. Matsumura, G. Hyoudou, M. Itoh, H. Kato, T. Nishioka, E. Matsuoka, H. Tou, T. Takabatake, and M. Sera, *J. Phys. Soc. Jpn.* **76**, 084716 (2007).
- [48] M. Shimizu, H. Amanuma, K. Hachitani, H. Fukazawa, Y. Kohori, T. Namiki, C. Sekine, and I. Shirotnani, *J. Phys. Soc. Jpn.* **76**, 104705 (2007).
- [49] K. Magishi, R. Watanabe, A. Hisada, T. Saito, K. Koyama, T. Saito, R. Higashinaka, Y. Aoki, and H. Sato, *J. Phys. Soc. Jpn.* **83**, 084712 (2014).
- [50] B. Nowak, O. Żogał, Z. Henkie, and M. B. Maple, *Solid State Commun.* **151**, 550 (2011).
- [51] M. Yogi, H. Niki, T. Kawata, and C. Sekine, *JPS Conf. Proc.* **3**, 011046 (2014).
- [52] K. Asaki, H. Kotegawa, H. Tou, S. Tatsuoka, R. Higashinaka, T. Namiki, and H. Sato, *J. Phys. Soc. Jpn.* **80**, SA033 (2011).
- [53] T. Moriya, *Prog. Theor. Phys.* **16**, 23 (1956).